• Why is dithering necessary?



- Why is dithering necessary?
 - To reproduce gray levels on binary displays



Laser printed image WITH dithering

Laser printed image WITHOUT dithering

• Is a pixel with value 255 twice as bright as another pixel with value 128?



- Is a pixel with value 255 twice as bright as another pixel with value 128?
 - No, 128 is darker than half the brightness of 255 because of the Gamma function
 - Displays are calibrated to use the standard gamma=2.2 $I(n) = (n/N)^{\gamma}$



How many levels are necessary for a smooth gradation W/O visible steps?



How many levels are necessary for a smooth gradation W/O visible steps?

- It depends on the dynamic range of a display
- Ideal case : exponential quantization

2% steps are most efficient because we cannot notice a change less than 2%:

$$0 \mapsto I_{\min}; 1 \mapsto 1.02I_{\min}; 2 \mapsto (1.02)^2 I_{\min}; \dots$$

120 steps are needed for 10:1 dynamic range because $(1.02)^{120} = 10.76$

240 steps are needed for 100:1 dynamic range High precision (e.g. 72bpp) is necessary for an HDR image

Perspective Lecture 3



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History of projection

- Ancient times: Greeks wrote about laws of perspective
- Renaissance: perspective is adopted by artists



History of projection

 Later Renaissance: perspective formalized precisely



da Vinci c. 1498

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Plane projection in photography

- This is another model for what we are doing
 - applies more directly in realistic rendering



Perspective

one-point:

projection plane parallel to a coordinate plane (to two coordinate axes) **two-point**:

projection plane parallel to one coordinate axis **three-point**:

projection plane not parallel to a coordinate axis



Carlbom & Paciorek 78

Perspective projection (normal)

- Perspective is projection by lines through a point
 - "normal" = image plane (film) perpendicular to view direction

h

α

- magnification determined by:
 - image height h
 - image plane distance d
 - object depth z
- f.o.v. $\alpha = 2 \operatorname{atan}(h/(2d))$
- -y' = dy/z
- "normal" case corresponds to common types of cameras

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View volume: perspective



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Field of view (or f.o.v.)

- The angle between the rays corresponding to opposite edges of a perspective image
 - easy to compute only for "normal" perspective
 - have to decide to measure vert., horiz., or diag.
- In cameras, determined by focal length
 - confusing because of many image sizes
 - for 35mm format (36mm by 24mm image)
 - 18mm = 67° v.f.o.v. super-wide angle
 - $28mm = 46^{\circ} v.f.o.v.$ wide angle
 - 50mm = 27° v.f.o.v. "normal"
 - 100mm = 14° v.f.o.v. narrow angle

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Field of view

Determines "strength" of perspective effects





close viewpoint wide angle prominent foreshortening Cornell CS4620 Fall 2008 • Lecture 3

far viewpoint narrow angle little foreshortening

Parallel projection

 Viewing rays are parallel rather than diverging



Multiview orthographic





front elevation



right elevation



FIGURE 2-1. Multiview orthographic projection: plan, elevations, and section of a building.

[Carlbom & Paciorek 78]

Multiview orthographic



- projection plane parallel to a coordinate plane
- projection direction perpendicular to projection plane

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Shifted perspective projection

- Perspective but with projection plane not perpendicular to view direction
 - additional parameter: projection plane normal
 - exactly equivalent to cropping out an off-center rectangle from a larger
 "normal" perspective
 - corresponds to view camera in photography



Why shifted perspective?

- Control convergence of parallel lines
- Standard example: architecture
 - buildings are taller than you, so you look up
 - top of building is farther away, so it looks smaller
- Solution: make projection plane parallel to facade
 - top of building is the same distance from the projection plane
- Same perspective effects can be achieved using post-processing
 - (though not the focus effects)
 - choice of which rays vs. arrangement of rays in image



camera tilted up: converging vertical lines



lens shifted up: parallel vertical lines

Specifying perspective projections

- Many ways to do this
 - common: from, at, up, v.f.o.v. (but not for shifted)
- One way (used in ray tracer):
 - viewpoint, view direction, up
 - establishes location and orientation of viewer
 - view direction is the direction of the center ray
 - image width, image height, projection distance
 - establishes size and location of image rectangle
 - image plane normal
 - can be different from view direction to get shifted perspective